

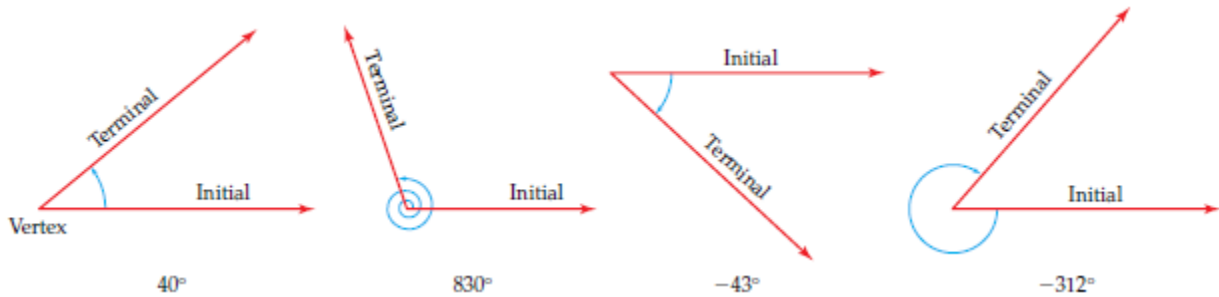
Off-Site Learning Packet Day 4

6-3 Day 1 Angles and Radian Measure

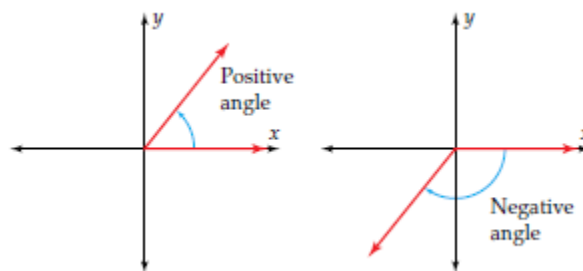
Extending Angle Measure

In geometry and triangle trigonometry, an angle is a static figure consisting of two rays that meet at a point. But in modern trigonometry, an angle is thought of as being formed dynamically by *rotating* a ray around its endpoint, the vertex. The starting position of the ray is called the initial side and its final position after rotation is called the terminal side.

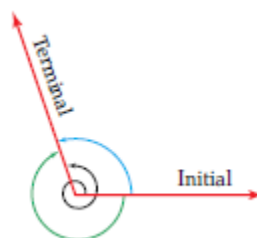
The amount the ray is rotated is the measure of the angle. Counterclockwise rotations have positive measure and clockwise rotations have negative measure.



An angle in the coordinate plane is said to be in standard position if its vertex is at the origin and its initial side is on the positive x-axis.



Angles formed by different rotations that have the same initial and terminal side are called coterminal.



Example 1: Coterminal Angles

Find three angles coterminal with an angle of 60° in standard position.

$$60 + 360 = 420^\circ$$

$$420 + 360 = 780^\circ$$

$$60 - 360 = -300^\circ$$

Arc Length

Arc – *unbroken part of a circle*

Central Angle – *an angle whose vertex is at the center of a circle*

Arc length can be calculated by considering an arc as a fraction of the entire circle. Suppose an arc in a circle of radius r has a central angle measure of θ .

$$\text{An arc of a circle is } \frac{\theta}{360} \quad \text{Circumference} = 2\pi r$$

$$\text{Length of arc: } l = \frac{\theta}{360} \cdot 2\pi r = \frac{\theta\pi r}{180}$$

Example 2: Finding an Angle Given an Arc Length

An arc in a circle has an arc length l which is equal to the radius r . Find the measure of the central angle that the arc intercepts.

$$r = l$$

$$r = \frac{\theta\pi r}{180} \quad 180r = \theta\pi r \quad 180 = \theta\pi$$

$$\theta = \frac{180}{\pi} = 57.3^\circ$$

Radian Measure

The angle found in Example 2 leads to another unit used in finding angle measure called *radian*.

Angle measurement in radians can be described in terms of the Unit Circle, which is the circle of radius 1 centered at the origin, whose equation is $x^2 + y^2 = 1$.

$$360^\circ = 2\pi \text{ radians}$$

$$1 \text{ radian} = \left(\frac{180}{\pi}\right)^\circ = 57.3^\circ$$

Converting Angle Measures	
DEGREES TO RADIANS	RADIANS TO DEGREES
Multiply the number of degrees by $\frac{\pi}{180}$	Multiply the number of radians by $\frac{180}{\pi}$

Example 3: Converting From Radians to Degrees

Convert the following radian measurements to degrees.

a) $\frac{\pi}{5}$

$$\frac{\pi}{5} \cdot \frac{180}{\pi} = \frac{180}{5} = 36^\circ$$

b) $\frac{4\pi}{9}$

$$\frac{4\pi}{9} \cdot \frac{180}{\pi} = \frac{720}{9} = 80^\circ$$

c) 6π

$$6\pi \cdot \frac{180}{\pi} = 1080^\circ$$

Example 4: Converting from Degrees to Radians

Convert the following degree measurements to radians.

a) 75°

$$75^\circ \cdot \frac{\pi}{180} = \frac{5\pi}{180}$$

b) 220°

$$220^\circ \cdot \frac{\pi}{180} = \frac{11\pi}{9}$$

c) 400°

$$400^\circ \cdot \frac{\pi}{180} = \frac{20\pi}{9}$$

Assessment:

Pg 441 #7-43 (odd)